

**Algorithm 1** **Power\_of\_2**(natural number **k**)

**Input:**  $k$  , a natural number

**Output:**  $k$ -th power of 2

**Algorithm:**

if  $k = 0$ , then return 1;

else return  $2 * \text{Power\_of\_2}(k - 1)$  .

By way of comparison, let us see how the same problem can be solved by an iterative algorithm.

**Algorithm 2** **Power\_of\_2**(natural number **k**)

**Input:**  $k$  , a natural number

**Output:**  $k$ -th power of 2

**Algorithm:**

int  $i, power$ ;

$i := 0$ ;

$power := 1$ ;

while(  $i < k$  ) {

$power := power * 2$ ;

$i := i + 1$ ;

}

return  $power$  .

**Algorithm 3: Even**(positive integer  $k$ )

**Input:**  $k$ , a positive integer

**Output:**  $k$ -th even natural number (the first even being  $0$ )

**Algorithm:**

int  $i, even$ ;

$i := 1$ ;

$even := 0$ ;

while(  $i < k$  ) {

$even := even + 2$ ;

$i := i + 1$ ;

}

return  $even$  .

**Algorithm 4 Natural**(a number  $x$ )

**Input:** A number  $x$

**Output:** "Yes" if  $x$  is a natural number, else "No"

**Algorithm:**

if  $x < 0$ , then return "No"

else

    if  $x = 0$ , then return "Yes"

    else return **Natural**(  $x - 1$  )